

UNIFORM CIRCULAR MOTION

UNIT 1- SECTION 3-
PHYSICS 3204

- Remember that centripetal force is the net force. That is the ΣF on an object.
- There are three different types of centripetal motion studied.

1. On an horizontal plane

$D = 2\pi r$ (circumference)

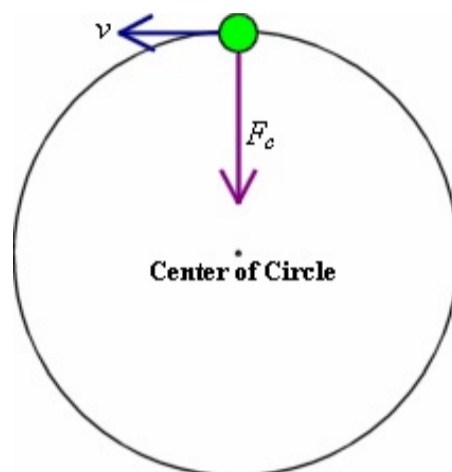
$$v = \frac{2\pi r}{T} \quad (T = \text{Period})$$

$$F_c = \frac{mv^2}{r}$$

$$a_c = 4\pi^2 r f^2$$

$$F_c = m4\pi^2 f^2$$

$$f = \frac{1}{T} \quad \text{Or} \quad f = \frac{\# \text{cycles}}{\text{time}}$$

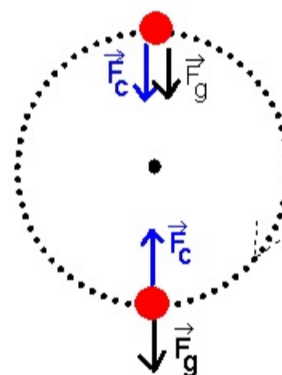


2. Vertical plane (use formulae from above)

For tension

$$F_{\text{net}} = T + F_g$$

$$F_c = T + F_g$$



- Note forces towards the center are considered to be positive and outside are negative.

TOP	BOTTOM
$F_c = T + F_G$	$F_c = T - F_G$

- Note make sure to look at the following questions:
 - \Rightarrow Bucket problem- minimum velocity to keep the bucket in centripetal motion (Tension = 0).
 - \Rightarrow Roller Coaster Problem the minimum velocity of to keep the roller coaster on the track (Force normal = 0).

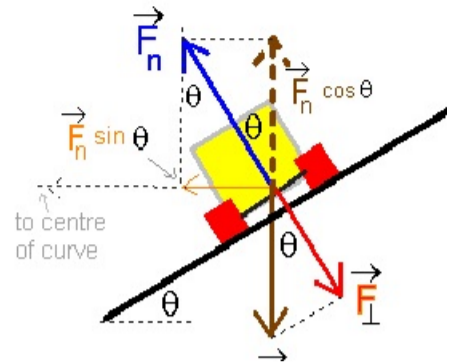
3) Banked curve:

$$F_C = F_n \sin\theta$$

$$F_C = \frac{mv^2}{r}$$

using the above two equations we get

$$r = \frac{v^2}{g \tan \theta} \quad \text{Or} \quad v = \sqrt{rg \tan \theta}$$



Note: If the turn is not banked, it is static friction that keeps the car on the road:

In the vertical direction, $F_n = mg$,

In the horizontal direction : $F_c = F_f$ (to keep the car from skidding off the curve)

$$F_c = F_f$$

$$\frac{mv^2}{r} = \mu F_n$$

$$\frac{mv^2}{r} = \mu mg \quad (\text{ divide by m on both sides})$$

$$\frac{v^2}{r} = \mu g \quad (\text{ divide by m on both sides})$$

Solve for v

$$v = \sqrt{rg\mu}$$

